

## Answers to L<sup>A</sup>T<sub>E</sub>X Exercises

### Exercise 1

Copy this file to your directory and look up how to process it in the local guide. Note how the input text file contains quite verbose instructions in plain text, which are the typesetting commands. [Use the Local Guide!]

### Exercise 2

**Outliers** are sample values which cause surprise in relation to the majority of the sample. This is not a pejorative term: outliers may be correct, but they should always be checked for transcription errors.

The sample mean can be upset completely by a single outlier: if any data value go to infinity, then so does the mean. This contrasts with the sample median, which is little affected by moving any single value to infinity. We say that the median is *resistant* to *gross errors* whereas the mean is not. In fact the median will tolerate up to 50% gross errors before is can be made arbitrarily large; we say its *breakdown point* is 50% whereas that for the mean is 0%.

```
\documentclass[12pt, a4paper]{article}
\usepackage{parskip,times}
```

```
\begin{document}
```

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### Exercise 3

I entered the room and—horrors—I saw both my father-in-law and my mother-in-law. The winter of 1484–1485 was one of discontent.

1

```
\begin{quote}
Frank wondered, "Is this a girl that can't say 'No!'?"
```

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Frank wondered, "Is this a girl that can't say 'No!'?"
\end{quote}
```

### Exercise 4

Refine the exercise 2, and try changing the type face of words and the type size of paragraphs.

### Exercise 5

Does `\Aschylus` understand `\Edipus`?

The smallest internal unit of `\TeX` is about 53.63A.

They took some honey and plenty of money wrapped up in a £5 note.

Elèves, refusez vos legons! Jetez vos chaînes!

Can you take a ferry from Oland to Åland.

Does `\AE` schylus understand `\OE` dipus?

The smallest internal unit of `\TeX` is about 53.63AA.

They took some honey and plenty of money wrapped up in a \pounds 5 note.

```
\E1\èves, refusez vos le\c cons! Jetez vos cha\! nes!
```

Can you take a ferry from \Oland to \AA land.

### Exercise 6

## Currencies 1 Jan 1992

London: New York:

£: \$ 1.8672      £: \$ 1.8655

£: DM 2.8369    \$: DM 1.5175

£: FFf 9.969080 \$: FFf 5.1845

2



**Exercise 15**

$$\bigvee (y \vee z) = (x \vee y) \vee (x \vee z).$$

$$(x \wedge y) \vee (x \wedge z) = (x \wedge (y \vee z)).$$

**Exercise 16**

$$+ 4 + 6 + \dots + 2n = n(n + 1).$$

$$2 + 4 + 6 + \dots + 2n = n(n + 1).$$

**Exercise 17**

$$\vec{f} \perp \vec{g} \text{ if and only if } \vec{f} \cdot \vec{g} = 0.$$

$$\vec{x} \perp \vec{y} \text{ if and only if } \vec{x} \cdot \vec{y} = 0 \text{ and only if } \vec{x} \cdot \vec{y} = 0.$$

**Exercise 18**

$$\vec{f} \neq \vec{g} \text{ if and only if } \vec{f} \cdot \vec{f} \neq \vec{g} \cdot \vec{g}.$$

$$\vec{x} \cdot \vec{y} \neq 0 \text{ if and only if } \vec{x} \text{ and } \vec{y} \text{ are not perpendicular.}$$

$$\vec{x} \cdot \vec{y} \neq 0 \text{ which is } \vec{x} \cdot \vec{y} \neq 0 \text{ if and only if } \vec{x} \text{ and } \vec{y} \text{ are not perpendicular.}$$

**Exercise 19**

$$\exists y \in \mathbb{R} \text{ such that } y > x.$$

$$\forall x \in \mathbb{R} \text{ there exists } y \text{ such that } y > x.$$

Note that `amssymb` must be included in the `usepackage` declaration at the beginning of the file in order to use `\mathbb{R}`.

**Exercise 20**

$$\frac{1}{\frac{1}{a} + \frac{1}{b} + \frac{1}{c}} = \frac{abc}{a+b+c}.$$

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the could be used instead of `\not=`

**Exercise 21**

What are the points where  $\frac{\partial^2 f}{\partial x^2} f(x, y) = \frac{\partial^2 f}{\partial y^2} f(x, y) = 0$ ?

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**Exercise 22**

$$e^x e^{-x} e^{i\pi} + 1 = 0 \quad x_0 \quad x_0^2 \quad x_0^2 \quad 2x^x.$$

$$e^x \quad e^{-x} \quad e^{i\pi} + 1 = 0 \quad x_0 \quad x_0^2 \quad x_0^2 \quad 2x^x.$$

**Exercise 23**

$$\Delta^2 f(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}.$$

$$\frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}.$$

**Exercise 24**

$$\lim_{x \rightarrow 0} (1 + x)^{\frac{1}{x}} = e.$$

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**Exercise 25**

The cardinality of  $(-\infty, \infty)$  is  $\aleph_1$ .

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**Exercise 26**

$$\lim_{x \rightarrow 0} x^x = 1.$$

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**Exercise 27**

$$\int_0^1 3x^2 dx = 1.$$

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**Exercise 28**

$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \sqrt{x^2 + y^2} e^{-\sqrt{x^2 + y^2}} dx dy = 0.$

**Exercise 29**

$\int_0^1 \int_0^1 \sqrt{x^2 + y^2} dx dy = \frac{1}{2} \ln 2 + \frac{1}{2} \sqrt{2}.$

**Exercise 30**

$\int_0^1 \int_0^1 e^{-x^2 - y^2} dx dy = \frac{1}{2} \sqrt{2} \operatorname{erf}\left(\frac{\sqrt{2}}{2}\right).$

**Exercise 31**

$\int_0^1 \int_0^1 \frac{1}{1 + x^2 + y^2} dx dy = \frac{1}{2} \left( \frac{\pi}{2} - \arctan 2 \right).$

**Exercise 32**

$\int_0^1 \int_0^1 |x - y| dx dy = \frac{1}{3}.$

**Exercise 33**

$\int_0^1 \int_0^1 \cos(2\theta) dx dy = \frac{1}{2} \cos 2\theta.$

**Exercise 34**

$\int_0^1 \int_0^1 \csc^2 x dx dy = -\cot x + C.$

**Exercise 35**

$\tan(2\theta) = \frac{1 - \tan^2 \theta}{2 \tan \theta}.$

**Exercise 36**

$$\begin{bmatrix} az & \dots & az \\ \vdots & \ddots & \vdots \\ za & \dots & za \end{bmatrix}$$

$\int_0^1 \int_0^1 \frac{1}{1 + x^2 + y^2} dx dy = \frac{1}{2} \left( \frac{\pi}{2} - \arctan 2 \right).$

**Exercise 37**

$f(y; \theta, \phi) = \exp\left\{y\theta - b(\theta) + c(y; \phi)\right\}$

A random variable  $Y$  has density

and its moment-generating function is  $M(t) = \int_0^1 \int_0^1 \exp\{t\theta - b(\theta) + c(y; \phi)\} f(y; \theta, \phi) dy d\theta$ .

A random variable  $Y$  has density  $f(y; \theta, \phi) = \frac{1}{a} \exp\left\{y\theta - b(\theta) + c(y; \phi)\right\}$  and its moment-generating function is  $M(t) = \int_0^1 \int_0^1 \exp\{t\theta - b(\theta) + c(y; \phi)\} f(y; \theta, \phi) dy d\theta$ .

**Exercise 38**

If  $Y_1, \dots, Y_r, C$  are random variables, show that

$$\sum_{j=1}^r Y_j - Y_r - C = \sum_{j=1}^{r-1} Y_j - Y_r - C.$$

(1)

```

\begin{cases}
X = 1/(4U - 1), V = U_1/X^2 & \text{if } U < 0.5, \\
X = 4U - 3, V = U_1 & \text{otherwise.}
\end{cases}

```

1. Generate independent uniforms  $U$  and  $U_1$ .
2. Set  $\left\{ \begin{array}{l} X = 1/(4U - 1), V = U_1/X^2 \\ X = 4U - 3, V = U_1 \end{array} \right.$  if  $U < 0.5$ , otherwise.
3. If  $V < 1 - 0.5|X|$  go to 5.
4. If  $V \geq (1 + X^2)^{1/2} - (1 + X^2)^{-1/2}$  go to 1.
5. Return  $X$ .

**Exercise 41**

$$\frac{\partial G}{\partial \lambda} = \lambda s(s-1) \frac{\partial s}{\partial \lambda}$$

**Exercise 40**

You could use `\mid`, but the spacing would be larger.

$$f(x_i | \lambda_i) = \lambda_i e^{-\lambda_i x_i}, \quad f(y_i | \lambda_i, \psi) = \lambda_i \psi e^{-\lambda_i \psi y_i}, \quad x_i, y_i \geq 0.$$

**Exercise 39**

```

\sum_{r,c} (\overline{x_{r,c}} - \overline{x_{..}})^2 + \sum_{r,c} (\overline{y_{r,c}} - \overline{y_{..}})^2
\overline{x_{r,c}} = \frac{1}{n} \sum_{i=1}^n x_{ri}
\overline{y_{r,c}} = \frac{1}{n} \sum_{i=1}^n y_{ri}

```

**Exercise 42**

```

\item If  $V < 1 - 0.5|X|$  go to 5.
\item If  $V \geq (1 + X^2)^{1/2} - (1 + X^2)^{-1/2}$  go to 1.
\end{cases}

```

$$h_i(t) = \lim_{\epsilon \rightarrow 0} \frac{P(T_i^+ \leq t + \epsilon) - P(T_i^+ \leq t)}{\epsilon}$$