Statistical Programming

Worksheet 5

1. Polynomials. Find the coefficients of the quintic polynomial f(x) for which

 $(f(2), f(3), f(4), f(5), f(6), f(7))^T = (3, 2, 1, 6, 95, 538)^T$

[Hint: set the problem up as a system of linear equations and use solve()].

2. Linear Models. The data in speed.txt (available on the course website) give the times in seconds recorded by the winners in the finals of various men's running events (200, 400, 800 and 1500 metres) at each of the 21 Olympic Games from 1900 to 2004, along with the heights above sea level of the different venues.

Read in the data and take a look at it. Calculate the average speed (in metres per second) of the winner of each race, and add this to the dataframe.

Fit the following models to the dataset

- (i) speed against $\log_2(\text{distance})$.
- (ii) speed against $\log_2(\text{distance})$, year and $\log_2(\text{altitude})$.

Fit model (i) twice using (a) the lm() command, and (b) using qr.solve().

3. Gram-Schmidt. One method for obtaining the QR decomposition of an $n \times p$ matrix A is to use the Gram-Schmidt process. The algorithm for this is below.

 \mathbf{end}

- (a) Implement the algorithm as a function in R.
- (b) Combine your answer to (a) and to Question 3 from Sheet 4 (recall it implemented a back-solving method) to construct a function for solving linear models from scratch. Apply the function to the data in question 2.
- (c) What is the complexity of this algorithm?