

Part A Simulation and Statistical programming HT14

Geoff Nicholls

Lecture 11: reference slides for matrices in R

## R commands for matrices and vectors

Here are some slides of R commands for matrices and vectors.  
Please refer back to them in the practical as needed.

## Vectors and Matrices in R

Matrices can be constructed using the functions `matrix()`, `cbind()` or `rbind()`.

```
matrix(data, nrow, ncol)
# data is a vector of nrow*ncol values
```

```
cbind(d1, d2, ..., dm)
# d1, ..., dm are vectors (columns)
```

```
rbind(r1, r2, ..., rn)
# r1, ..., rn are vectors (rows)
```

## Accessing elements

If  $X$  is a matrix we can access the element in the  $i$ th row and  $j$ th column using  $X[i,j]$

We can access the  $i$ th row using  $X[i,]$ , and the  $j$ th column using  $X[,j]$ .

These commands result in an answer that is a vector with no dimension information kept. If we want to maintain the result as a row or column vector we use the option `drop = FALSE` i.e.  $X[i, ,drop = FALSE]$  and  $X[,j,drop = FALSE]$

If we want to find which elements satisfy a certain property we can use the `which()` command.

```
which(X >= 0, arr.ind = TRUE)
```

## Matrix properties

There are a few useful functions that return basic properties of matrices

`dim()` returns the number of rows and columns

`det()` returns the determinant of a square matrix

`diag()` returns the diagonal entries of a matrix

OR turns a vectors into a diagonal matrix.

`sum(diag())` can be used to calculate the trace.

`t()` returns the transpose of a matrix

`upper.tri()` returns a matrix of logical elements with **TRUE** for the upper triangular elements.

`lower.tri()` returns a matrix of logical elements with **TRUE** for the lower triangular elements.

`eigen()` Computes eigenvalues and eigenvectors of real or complex matrices.

## Matrix arithmetic

<code>X + Y</code>	element-wise addition (matrices must conform)
<code>X + 2</code>	addition of 2 to each element of <b>X</b>
<code>X * Y</code>	element-wise multiplication (matrices must conform)
<code>X * 2</code>	multiplication of each element of <b>X</b> by 2
<code>X %*% Y</code>	matrix multiplication (matrices must conform)
<code>crossprod(Y,X)</code>	calculates $Y^T X$ efficiently
<code>crossprod(Y)</code>	calculates $Y^T Y$
<code>solve(X)</code>	returns the inverse of a square matrix.
<code>solve(X,b)</code>	Solves a system of linear equations $X\theta = b$
<code>backsolve(A,b)</code>	Solves a system of linear equations $A\theta = b$ where the coefficient matrix $A$ is upper or lower triangular.