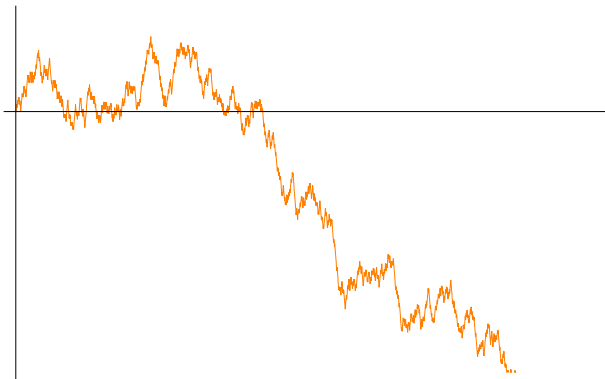


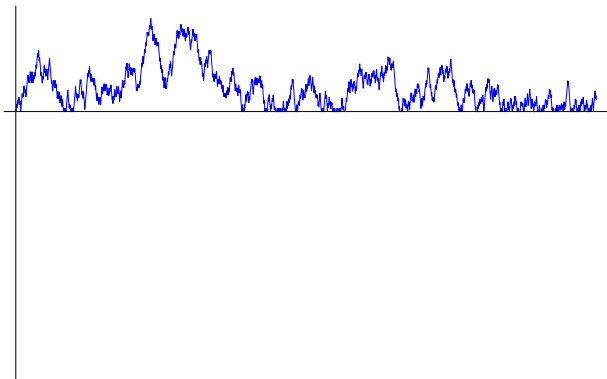
# Lecture 3

# Component sizes and surplus edges



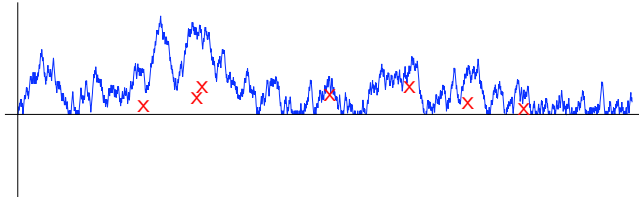
[Picture by Louigi Addario-Berry]

# Component sizes and surplus edges



[Picture by Louigi Addario-Berry]

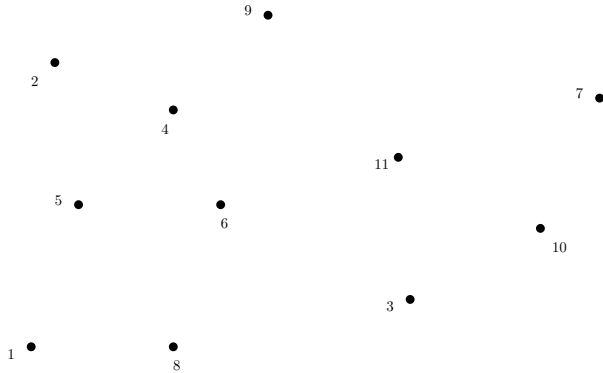
# Component sizes and surplus edges



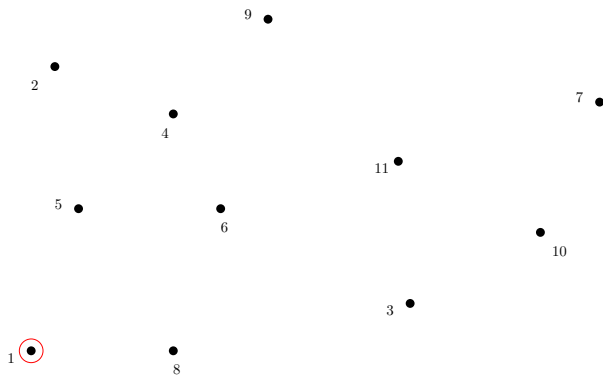
[Picture by Louigi Addario-Berry]



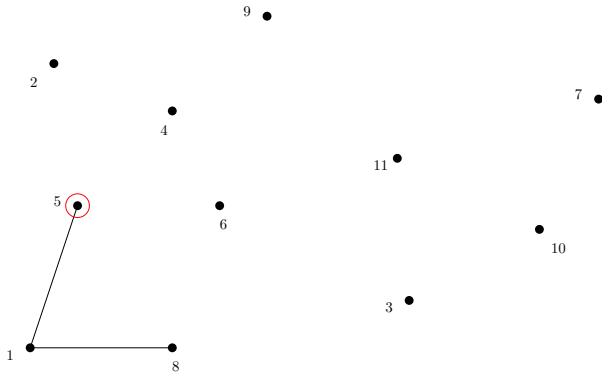
## Critical random graph: depth-first walk



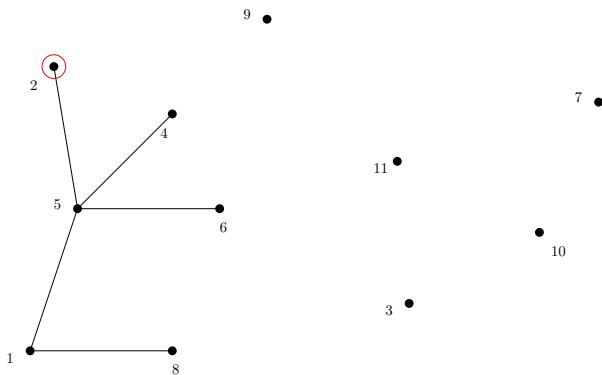
## Critical random graph: depth-first walk



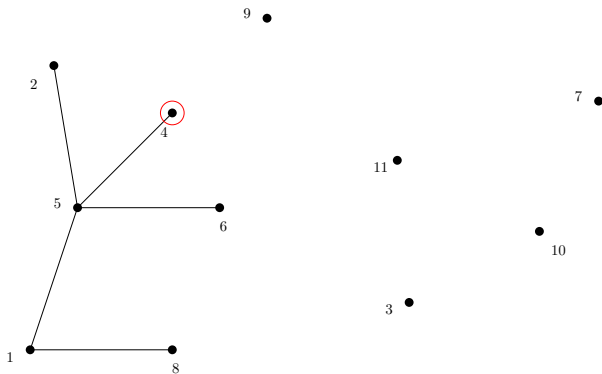
## Critical random graph: depth-first walk



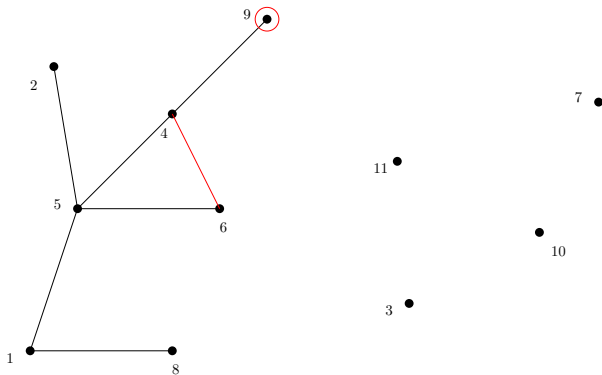
## Critical random graph: depth-first walk



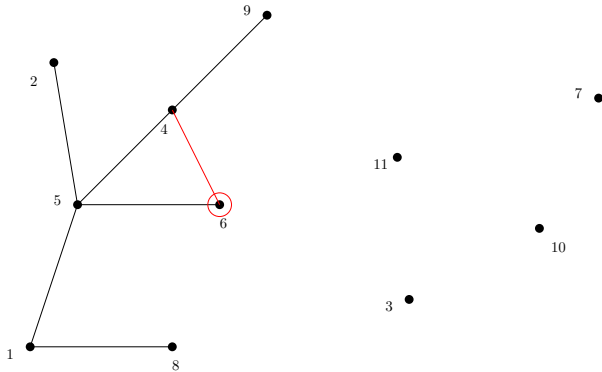
## Critical random graph: depth-first walk



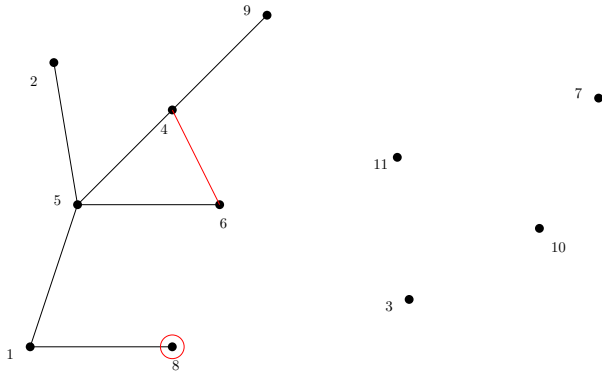
## Critical random graph: depth-first walk



## Critical random graph: depth-first walk

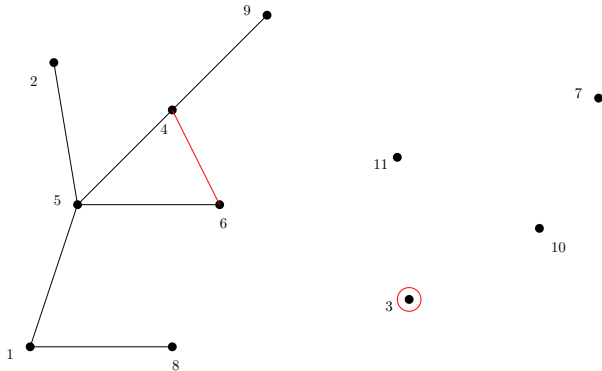


## Critical random graph: depth-first walk

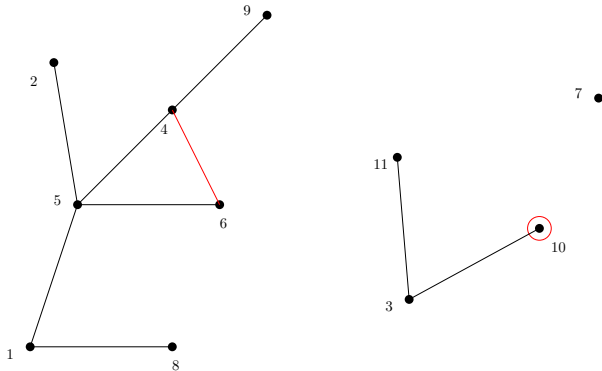




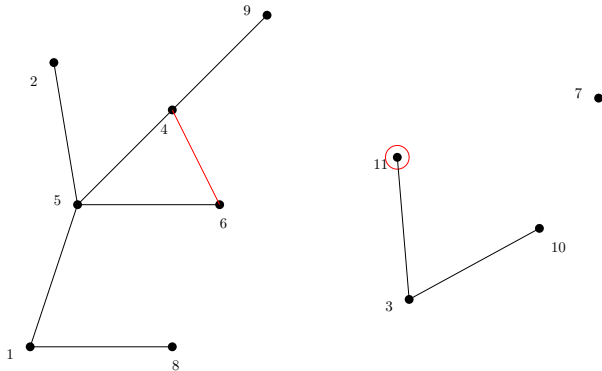
## Critical random graph: depth-first walk



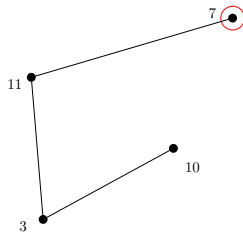
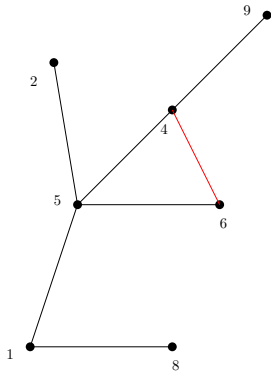
## Critical random graph: depth-first walk



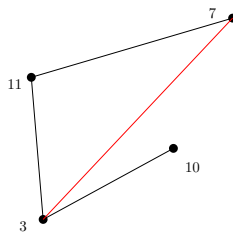
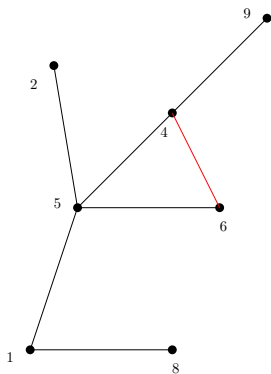
## Critical random graph: depth-first walk



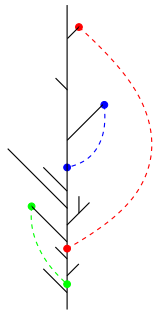
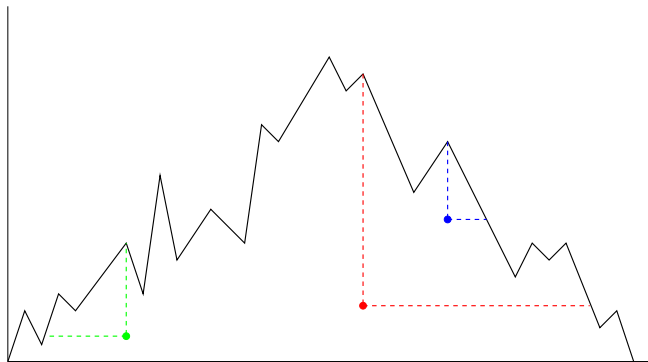
## Critical random graph: depth-first walk

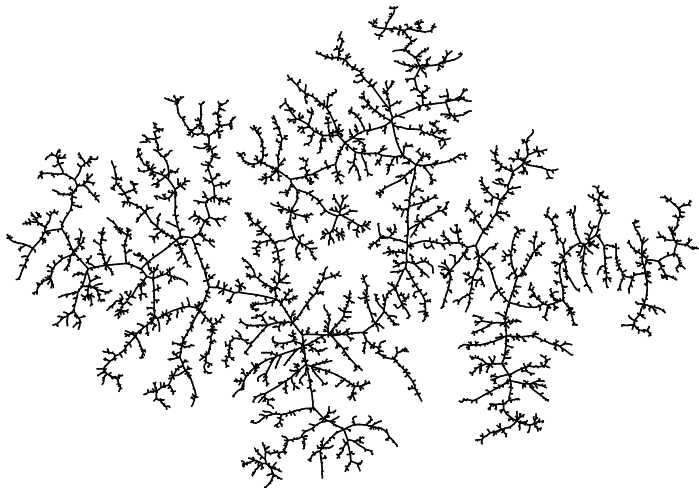


## Critical random graph: depth-first walk



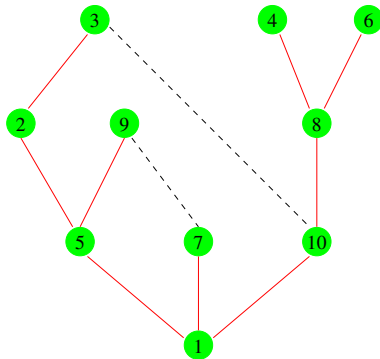
## Vertex identifications





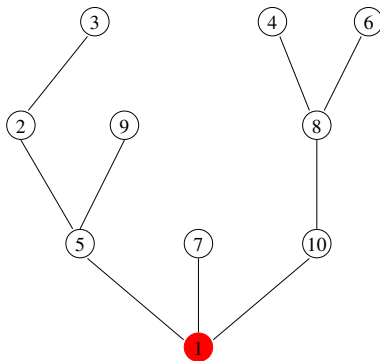
[Picture by Nicolas Broutin]

## Depth-first tree



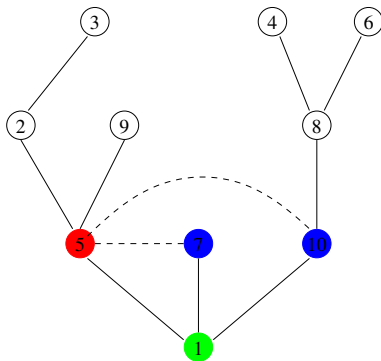


## Depth-first walk and permitted edges



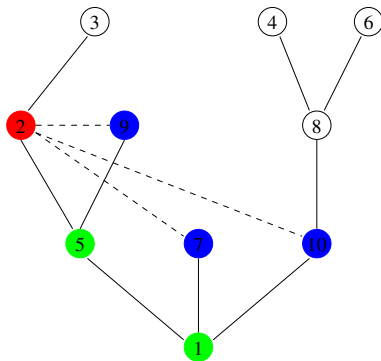
Step 0:  $X(0) = 0$ .

## Depth-first walk and permitted edges



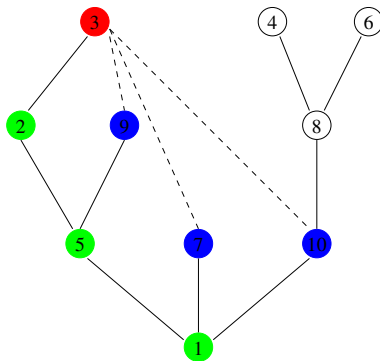
Step 1:  $X(1) = 2$ .

## Depth-first walk and permitted edges



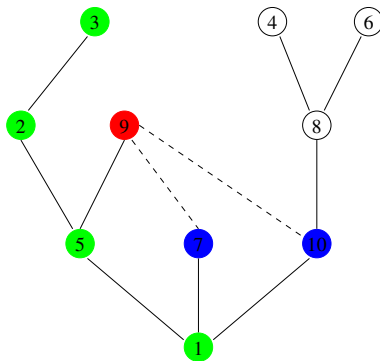
Step 2:  $X(2) = 3$ .

## Depth-first walk and permitted edges



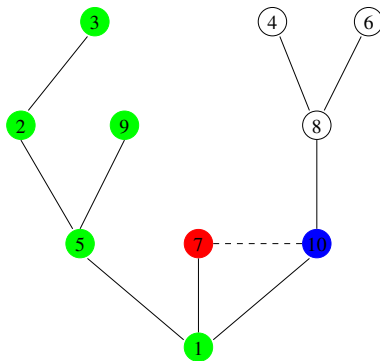
Step 3:  $X(3) = 3$ .

## Depth-first walk and permitted edges



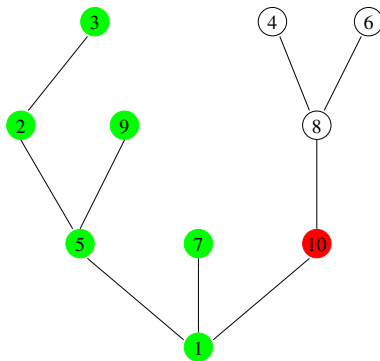
Step 4:  $X(4) = 2$ .

## Depth-first walk and permitted edges



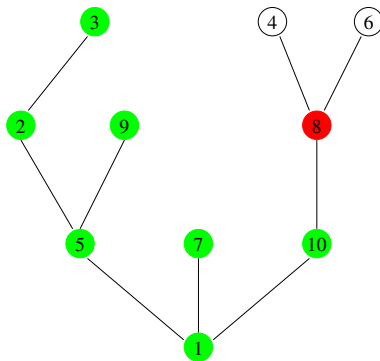
Step 5:  $X(5) = 1$ .

## Depth-first walk and permitted edges



Step 6:  $X(6) = 0$ .

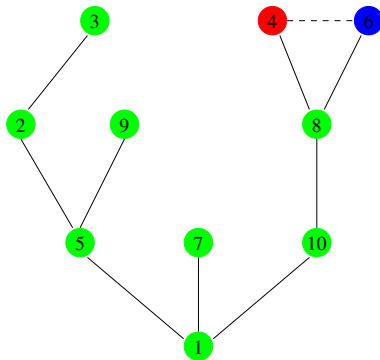
## Depth-first walk and permitted edges



Step 7:  $X(7) = 0$ .

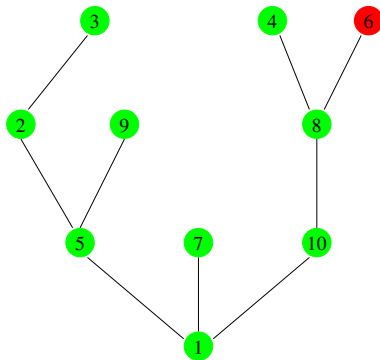


## Depth-first walk and permitted edges



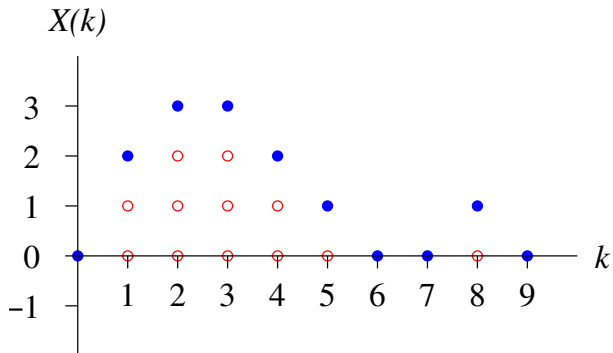
Step 8:  $X(8) = 1$ .

## Depth-first walk and permitted edges

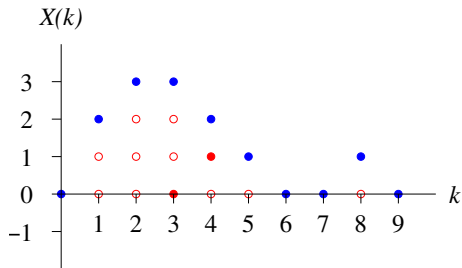
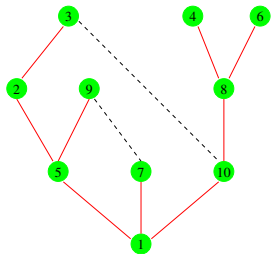


Step 10:  $X(9) = 0$ .

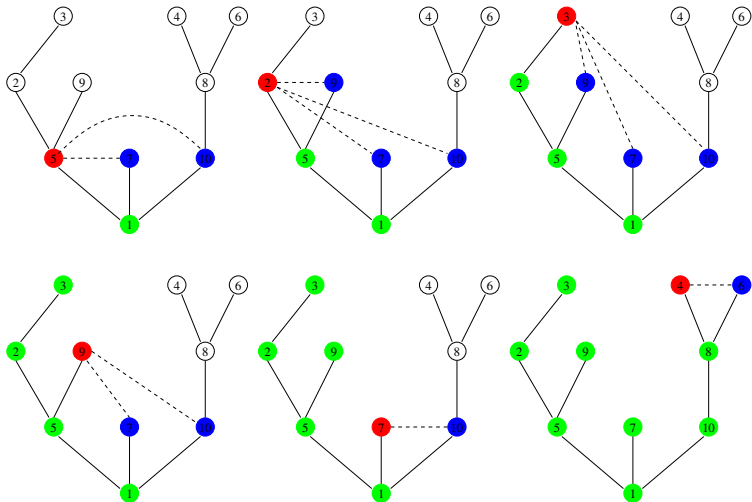
# Area



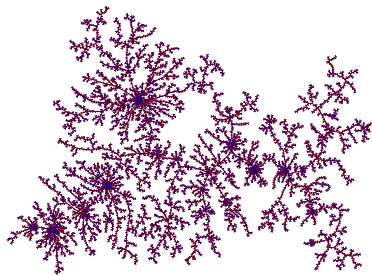
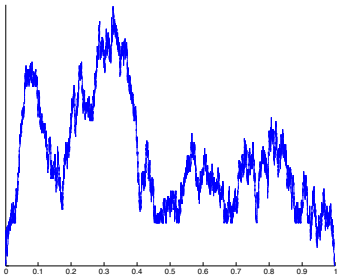
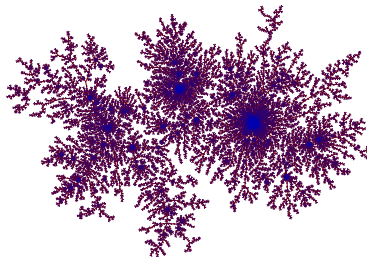
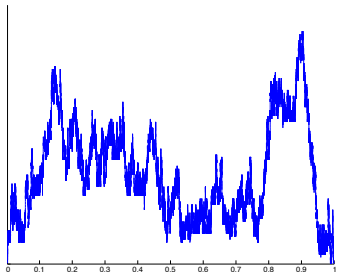
## Surplus edges



## Surplus edges



# $\alpha$ -stable trees ( $\alpha = 1.1$ and $\alpha = 1.5$ )



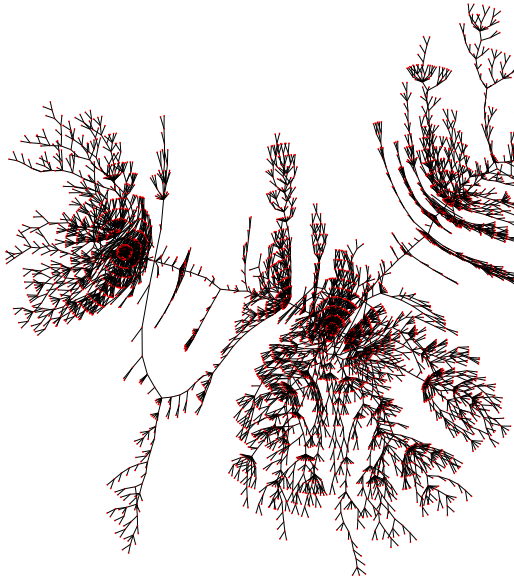
[Pictures by Igor Kortchemski]

# Heavy-tailed configuration model, $\alpha = 1.8$



[Picture by Delphin Sénizergues]

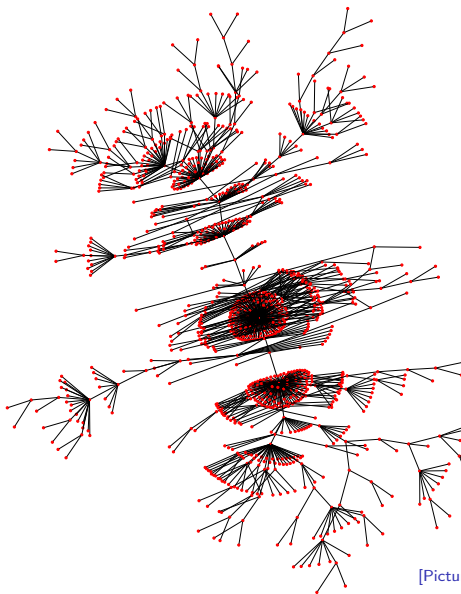
## Heavy-tailed configuration model, $\alpha = 1.5$



[Picture by Delphin Sénizergues]

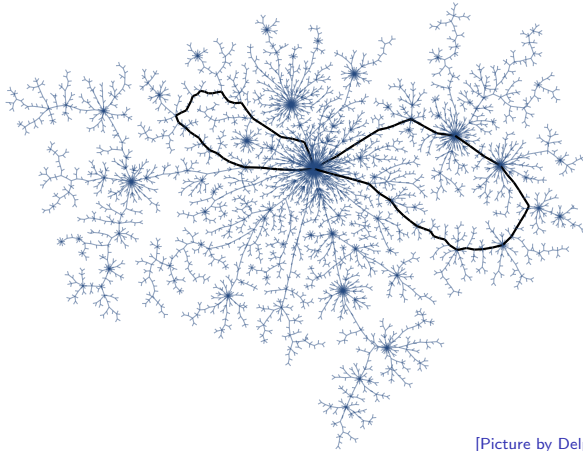


## Heavy-tailed configuration model, $\alpha = 1.2$



[Picture by Delphin Sénizergues]

Stable graph,  $\alpha = 1.5$



[Picture by Delphin Sénizergues]