

# MCMC INTEGRATION OVER EVOLUTIONARY HISTORIES OF METABOLIC NETWORKS

*Hugo Fernandes  
Hugo Martins  
Ricardo Pinho  
Rodrigo Liberal*

# The Project

- Goals

- Phylogenetic trees aka Probability of data  $P_t(N1, N2)$

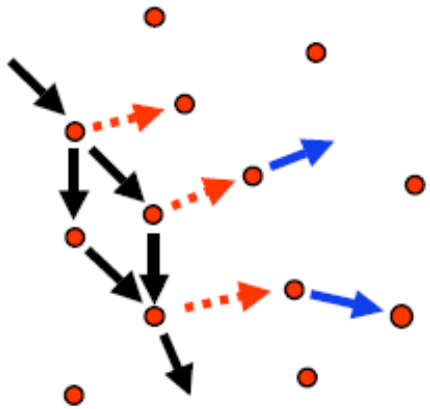


- Motivation

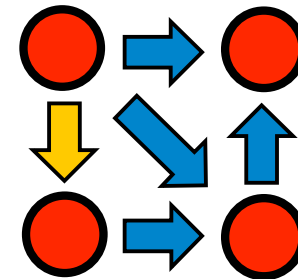
- sequence alignment vs metabolic network alignment  
(via evolutionary models)

# Metabolic Pathways as graphs

nodes = metabolites, edges = reactions



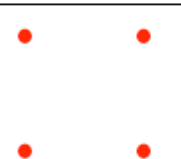
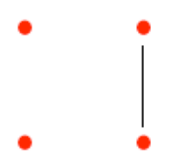
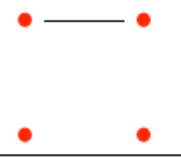
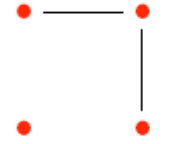
Black arrows:  
'core'  
metabolism  
Red arrows:  
'deletable' edges  
Blue arrows:  
'addable' edges



# Markov chains

- Evolution of Metabolic Pathways as a Markovian process  $P_t(N_1, N_2) = P(N_1)P_t(N_1 \rightarrow N_2)$

$$\frac{dP(t)}{dt} = QP(t) \quad P(t) = e^{Qt}$$

Network	Graph Structure
$N_1$	
$N_2$	
$N_3$	
$N_4$	

$Q(N_i \rightarrow N_j)$	$N_1$	$N_2$	$N_3$	$N_4$	...
$N_1$	$-\sum_j q_{1j}$	$\lambda$	$\lambda$	0	...
$N_2$	$\mu$	$-\sum_j q_{2j}$	0	$\lambda$	...
$N_3$	$\mu$	0	$-\sum_j q_{3j}$	$\lambda$	...
$N_4$	0	$\mu$	$\mu$	$-\sum_j q_{4j}$	...
...	...	...	...	...	...

# Computationally unfeasible

$n$	Number of all graphs with $n$ nodes	Number of states
1	1	1
2	2	2
3	8	8
4	64	61
5	1024	969
6	32768	31738
7	2097152	2069964
8	268435456	267270033
9	68719476736	68629753641
10	35184372088832	35171000942698

Table 1: Number of possible states of the Markov Chain for networks of size  $n$ .

# 0. Network Parsimony



MCMC**N**!

- ▣ Assessing distances between networks
- ▣ (Number of indels, time derived from insertion and deletion rates)

→ (white board)

# 1. Monte Carlo

- ▣ Monte Carlo methods to deal with large metabolic networks

MCMCMHMB!

→ (white board)

## 2. Sampling sub-graphs



MCMCWN!

→ (white board)

# Future Prospects



- ❑ Weighting the edges that stray from the core metabolism
- ❑ Fitness - better alignment or evolution for evolution's sake (without alignment)
- ❑ Parameter estimation
- ❑ Non uniform distributions (e.g. preferential attachment)
- ❑ Chemical equilibrium constant
- ❑ Meta-evolubility: Meta graph with meta grammar