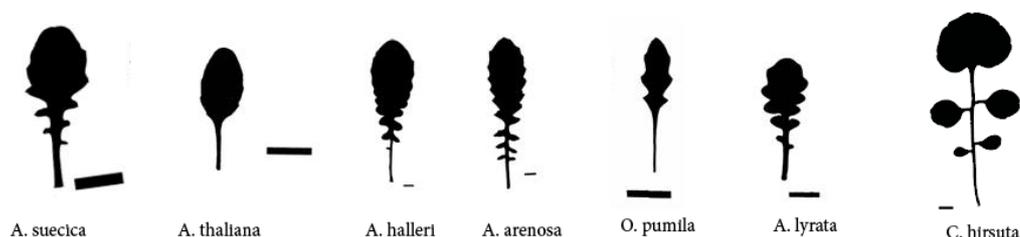




model organism *Arabidopsis thaliana*. The leaf shapes of the six species we will study represent all three types of leaf morphologies discussed i.e. fully dissected, lobed, and unlobed. We will develop and compare methodologies aiming to accurately capture and quantify leaf diversity in a representative sample of our species. This information together with knowledge about the phylogenetic relationships of the species we study will allow us to mathematically approximate and understand the precise shape transitions that produced divergent leaf shapes during crucifer evolution.



The data consists of several samples of each leaf outline (as above) with a known evolutionary tree. The leaf shape outlines will need to be converted to a set of data points from which the 1d Gaussian Process, used to model the evolution, can be inferred. This is well established as a procedure (for example, Rasmussen and Williams (2006)).

A key challenge to be solved is that leaf shapes can vary considerably owing to the presence of different numbers or orders of repeated shape elements such as lobes or leaflets. Such differences make it difficult to utilize conventional shape analysis methods many of which rely on investigating covariance of homologous parts within a structure. We will therefore aim to quantify leaf shape variation without the strict need to fix homologous points. Rather we will base our study on investigating the global properties of the curves that correspond to our leaf outlines.

### ***Models to be used***

The starting point will be the Jones and Moriarty (2011) model. This might be called “evolutionary functional data analysis” and extends sequence phylogenetics to functions (with co-domains of arbitrary dimension) by explaining how Gaussian Processes (like Random Walks and the Ornstein-Uhlenbeck process) can be put on phylogenies (it can also be viewed as a non-parametric approach to shape evolution). We will make a simple approximation that (after eliminating symmetries) the leaf edge can be treated as a function on 1-d which has been wrapped around a canonical leaf shape.

While treating leaf shapes as simple functions is a start, it clearly fails to capture the fact that biology can allow repeat units (developmental patterning through KNOX-genes – relatives of hox genes). To deal with this, we suggest a fusion of two approaches: a land-mark-free functional approach (to deal with smaller fluctuations in leaf shape) and one involving discrete characters (to capture the repeat patterning allowed by developmental genes). The students will explore both drastic changes in gene activity such as presence or absence of gene expression in leaves and subtler gene expression modifications within the functional framework. Such an approach does not have precedent and would be very cutting edge (it would also be useful for the study of protein shape evolution).

An alternative route is to really treat the leaf as a shape (rather than as a function) and help develop new land-mark-free and Bayesian non-parametric techniques for shape evolution. This is also a brand-new area and involves fusing the approaches in Holm et al. (2005,2009) with those in Jones and Moriarty (2011).

### ***The project***

The project would explore the applications of the above models to leaf shapes, by considering the following questions.

1. ***Can the model reconstruct the known evolutionary tree from the leaf shape data?*** Jones and Moriarty (2011) develop methods for constructing evolutionary trees given an underlying Gaussian Process evolutionary model. Clearly the model will be inappropriate for the problem if the evolutionary tree reconstructed is a poor representation of the true evolutionary tree.

2. **What do the inferred ancestral leaves look like?** Do these lie within biological reason? How do these leaf shapes change when using the true evolutionary tree as opposed to the inferred evolutionary tree? Again, this would also give insights to the appropriateness of the model.
3. **How stable is the model?** The data contains several samples of each leaf type. How do the inferred evolutionary tree and corresponding ancestral leaves change with the different samples? In the same vein, how much noise can be permitted in the data to still get strong inferences?

Looking at these questions will hopefully provide insights into both the process of leaf shape evolution and the model of Gaussian Processes for shape evolution modelling.

### ***Project Plan***

-Organise the data (leaf shapes and phylogenies) and undertake appropriate reading.  
 -Implement a simple version of the Jones and Moriarty (2011) algorithm and apply to leaf edges.-

Consider extensions:

- 1) possible integrations of evolutionary functional data analysis with discrete characters.
- 2) consider leaf shape evolution as a trajectory in shape space and make connections with the work of Holm et al. (2005,2009).

**Skills needed** – the project uses biology (ability to read literature about molecular biology of leaves), statistical and stochastic modelling and ability to efficient implementation of models/simulations.

## **References**

### **Key references**

#### **Gaussian Processes**

- [1] Jones and Moriarty, (2011). Evolutionary Inference for Functional Data: Using Gaussian Processes on Phylogenies to Study Shape Evolution. <http://arxiv.org/abs/1004.4668>
- [2] Rasmussen, C. and Williams, C. (2006). *Gaussian Processes for Machine Learning, Sections 2.1-2.3*. MIT Press. <http://www.gaussianprocess.org/gpml/chapters/RW.pdf>
- [3] [http://videlectures.net/gpip06\\_mackay\\_gpb/](http://videlectures.net/gpip06_mackay_gpb/)
- [4] [http://videlectures.net/mlss07\\_rasmussen\\_bigp/](http://videlectures.net/mlss07_rasmussen_bigp/)

#### **Leaf Shape Evolution**

- [5] Piazza et al., (2010). Arabidopsis thaliana Leaf Form Evolved via Loss of KNOX Expression in Leaves in Association with a Selective Sweep. *Current Biology* **20**, 1-6.
- [6] Hay and Tsiantis, (2006). The genetic basis for differences in leaf form between Arabidopsis thaliana and its wild relative Cardamine hirsuta. *Nature Genetics* **38**, 942-7.
- [7] Klingenberg (2010). Evolution and development of shape: integrating quantitative approaches. *Nat. Rev. Genet.* **11**, 623–635.
- [8] <http://www.plantcell.org/site/teachingtools/TTPB2.xhtml>
- [9] <http://www.plantcell.org/site/teachingtools/TTPB3.xhtml>

### **Supplementary references**

Gunz (2009) Early modern human diversity suggests subdivided population structure and a complex out-of-Africa scenario

Comparison of cranial ontogenetic trajectories among great apes and humans Philipp Mitteroeckera\*, Janssens et al. (2006) Quantitative and predictive model of transcriptional control of the *Drosophila melanogaster* even skipped gene *Nature Genetics* - 38, 1159 - 1165

Grenander and Miller (2007) Pattern Theory - From Representation to Inference OUP

Jonke et al. (2007) Secular trends in the facial skull from the 19th century to the present, analyzed with geometric morphometrics *American Journal of Orthodontics and Dentofacial Orthopedics* 132.1.63-70  
 Klingenberg (2010) “ Evolution and development of shape: integrating quantitative approaches” *Nat. Rev. Genet.* 11, 623–635

Lockwood et al.(2004) Morphometrics and hominoid phylogeny: Support for a chimpanzee–human clade and differentiation among great ape subspecies *PNAS* 101.13 4356–4360

Mardia and Dryden (1998) *Shape Analysis* Wiley

Mjolsness E, Sharp DH & Reinitz J (1991). A connectionist model of development. *J Theor Biol* 152: 429-453

Murray (2002), *Mathematical Biology 4<sup>th</sup> ed.*, Springer

Evolutionary Morphing David F. Wiley

Polly, D 2008, "Developmental Dynamics and G-Matrices: Can Morphometric Spaces be Used to Model Phenotypic Evolution?" *Evol. Biol.* 35, 83-96

Turing, *The chemical basis of morphogenesis*, Phil. Trans. Roy. Soc. Lond. B237, 37 (1952)

Wolpert (1969) Positional information and the spatial pattern of cellular differentiation. *J.Theoret.Biol.*, 25, 1 47325 36

<http://www.isbe.man.ac.uk/~bim/>

<http://graphics.idav.ucdavis.edu/research/projects/EvoMorph>D. Holm, T. Ratnanather, A. Trouvé, L.

Younes: Soliton Dynamics in Computational Anatomy, *Neuroimage* (2005) D. Holm, A. Trouvé

and L. Younes . "The Euler Poincare Theory of metamorphosis". *Quartely J. Applied Mathematics* (2009)